



As I understand it, I can conceive of all the distances shown as lengths of rods. Let's say that O has laid off a rod of length  $x$  to the position of an event in his frame that occurs at  $x$  at time  $t$  and then laid off another of length  $vt$  that represents the position of O relative to him---in his own frame. Let's also say that O' has laid off the rods  $x'$  and  $vt'$  in his own frame to represent these same lengths.

Now the conventional derivation seems to run like this. Letting  $\gamma = \frac{1}{\sqrt{1 - (v^2 / c^2)}}$ , O

perceives that  $x = \frac{1}{\gamma} x' + vt$ . Solving for  $x'$  gives  $x' = \gamma(x - vt)$ . My question is this:

couldn't we equally well say that  $x' = \frac{1}{\gamma}(x - vt)$ ? The rationale here is that observer O could just as well have laid off a rod of length  $x - vt$  in his frame and this *distance* would be modified by the length contraction factor  $1/\gamma$  as perceived by O'.

In fact, the "correct" derivation first given above seems to give fallacious results if we substitute  $t = 0$  because this says that  $x' = \gamma x$  at that instant---which flies in the face of length contraction. It seems to say that a length is dilated like a time interval.

I think the key issue that is befogging my mind is this. If there is a rod in the unprimed system of length  $L$ , then O' will perceive its length to be  $L' = \frac{1}{\gamma} L$ . Solving this gives  $L = \gamma L'$ . However, if O' has *laid off* a distance on his axis of  $L'$ , then O should actually measure it to be  $L = \frac{1}{\gamma} L'$ , shouldn't he? The issue here seems to be whether or not the observer actually marks off a distance equal to the length he has measured.

I'm sure I am confused on this issue, but I really am unable to see the difference between the two approaches. Can you help?

Thanks a lot.

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